

# THE INVESTIGATION OF THE RELATIONSHIP ELECTRONIC ENERGY ~ [VIBRATIONAL FREQUENCY]<sup>2</sup> X [INTERNUCLEAR DISTANCE]<sup>2</sup>, FOR CHEMICALLY ALIKE MOLECULES

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## ABSTRACT

The first author has previously established the following relationship between the *minimum electronic energy*  $E_{\min}$ , and the *lowest vibrational frequency*  $\omega_{\min}$  at this energy level, in regards to various *vibrational electronic states* of a given diatomic molecule:  $E_{\min} = 4\pi^2 M_0 g_k \omega_{\min}^2 r_{\min}^2$ . Here  $M_0$  is the *reduced mass* of the molecule,  $r_{\min}$  the *internuclear distance* associated with  $\omega_{\min}$ , and  $g_k$  a *dimensionless coefficient* usually around *unity*, insuring the equality; for electronic states configured alike, we expect the coefficient  $g_k$ , to remain practically the same. This essentially discloses an interesting architecture of diatomic molecules.

## INTRODUCTION

It was the author's original idea that the *special theory of relativity* imposes that, already at *rest*, the "*period of time*"  $T_0$ , the "*characteristic length*"  $R_0$ , the "*clock mass*"  $M_0$  to be associated with the internal dynamics of an atomistic or molecular wave-like object, and the total energy  $E_0$ , making the basis of the dynamics in question, ought to relate to each other in a given manner.<sup>1, 2, 3, 4, 5, 6, 7, 8</sup> More fundamentally, based on the *orchestration of electric charges*, these quantites are expected to be related to each other *two by two*, in just a unique way.<sup>9, 10, 11</sup>

The cancellation of electric charges from the expressions in question, ultimately leads to a *compact relationship*, between the four quantites of interest.

In this article we are going to provide a *direct derivation* of this interesting *compact relationship*.

Thus let  $E(r)$  be the *electronic energy of the molecule*, at a given state, with respect to the *internuclear distance*  $r$ .

$E(r)$  can be as usual, expressed, in terms of the *force constant*  $k_{\min}$ , associated with  $\omega_{\min}$  as,<sup>12</sup>

$$E(r) = E_{\min} + \frac{1}{2} k_{\min} (r - r_{\min})^2 . \quad (1)$$

It should be emphasized that this relationship, does not display *characteristics* such as "*anharmonicity*" and "*dissociation*"; but in this work we are dealing with only *the lowest vibrational level of the states* of concern. Thus, even when we look at an *excited electronic state*, Eq.(1) is quite valid, in regards to the *lowest vibrational level* of it.

$E(r)$  vanishes at the *abscissa*  $r_{00}$ , which we can define with respect to  $r_{\min}$ , as

$$r_{00} = p r_{\min} \text{ [value which makes } E(r), \text{ vanish] ;} \quad (2)$$

$p$  is an *unknown parameter* at this stage, though it appears to be roughly around 2.

Eqs.(1) and (2), provide us with the possibility of expressing  $E_{\min}$ , as

$$E_{\min} = \frac{1}{2} k_{\min} (p - 1)^2 r_{\min}^2 . \quad (3)$$

Next we define a quantity  $g_k$  as,

$$g_k = \frac{(p-1)^2}{2} . \quad (4)$$

Thus using the familiar expression,

$$\omega_{\min} = \frac{1}{2\pi} \sqrt{\frac{k_{\min}}{M_0}} , \quad (5)$$

we can *finally* arrive at our target relationship:

$$E_{\min} = 4\pi^2 M_0 g_k \omega_{\min}^2 r_{\min}^2 . \quad (6)$$

Note that Eq.(4) depicts two values for  $p$ , and in fact, there are two roots  $r_{00}$ , fulfilling Eq.(2).

We expect Eq.(6) to be valid not only regarding the electronic states of a given molecule, but also regarding the ground states of *chemically alike molecules*, for which we expect  $g_k$  to remain practically constant.

Let then  $E_0$  be the *magnitude of the ground state electronic energy*,  $\omega_0$  the *lowest vibration frequency* at  $E_0$ , and  $r_0$  the *ground state internuclear distance* of the molecule of concern.

Eq.(6) then becomes

$$E_0 = 4\pi^2 M_0 g_k \omega_0^2 r_0^2 . \quad (7)$$

Thus, we conjecture that the plot of  $E_0$  versus  $\omega_0^2 r_0^2$ , should come out as a *straight line* for *chemically alike molecules*, the slope of which furnishes the coefficient  $g_k$ .

We can equally write

$$T_0 = 2\pi \sqrt{\frac{g_k M_0}{E_0}} r_0 \quad (8)$$

where  $T_0$  is the inverse of  $\omega_0$ .

This equation suggests that, for *chemically alike molecules*, the period of vibration  $T_0$ , should behave proportionally to  $[\sqrt{M_0/E_0} r_0]$ .

We have calculated the electronic ground state energy  $E_{0AB}$ , of the diatomic molecule AB, in consideration, from

$$E_{0AB} = I_{0A} + I_{0B} + D_{0AB} , \quad (9)$$

where  $D_{0AB}$  is the *dissociation energy* of the molecule AB, and  $I_{0A}$  and  $I_{0B}$  are respectively the *ionization energies of the atoms*, A and B.

The attached tables and figures successfully display our prediction for all of the diatomic molecules, reassembled on the basis of their *chemical similarities*.

For each chemical family of concern,  $g_k$  is calculated and presented in Table 19.

**Table 1**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^3 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
H <sub>2</sub>	0,24	0,5	0,74	31,64	2,58	0,26
Li <sub>2</sub>	2,89	3,51	2,67	11,81	1,99	0,03
Na <sub>2</sub>	6,34	11,49	3,08	11,01	2,01	0,02
K <sub>2</sub>	10,88	19,49	3,92	9,19	1,91	0,07
NaK	8,06	14,48	3,50	10,03	1,92	0,06
NaRb	9,54	17,86	2,64	4,40	1,79	0,13
Rb <sub>2</sub>	18,06	42,47	4,21	9,64	1,96	0,04
Cs <sub>2</sub>	23,91	66,47	4,65	12,55	2,22	0,08
<b>Average</b>					2,04	0,09

**Table 2**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^3 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
N <sub>2</sub>	0,43	7,00	1,09	190,53	2,06	0,02
P <sub>2</sub>	1,29	15,49	1,89	125,87	1,94	0,04
PN	0,75	9,65	1,49	158,29	2,05	0,01
<b>Average</b>					2,02	0,02

**Table 3**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^3 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
O <sub>2</sub>	0,64	8,00	1,21	102,56	1,90	0,13
S <sub>2</sub>	1,39	15,99	1,89	72,46	1,60	0,06
Se <sub>2</sub>	2,57	39,97	2,15	82,22	1,71	0,02
Te <sub>2</sub>	4,00	63,83	2,59	58,35	1,48	0,12
SO	0,90	10,66	1,49	86,43	1,72	0,03
<b>Average</b>					1,67	0,07

**Table 4**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
F <sub>2</sub>	11,21	9,50	1,44	37,59	15,50	0,28
Cl <sub>2</sub>	17,96	17,49	1,99	28,4	11,50	0,05
Br <sub>2</sub>	31,15	39,96	2,28	25,59	10,93	0,09
I <sub>2</sub>	46,87	63,47	2,67	22,44	10,44	0,10
BrF	15,04	15,35	1,76	31,42	12,23	0,01
ClF	12,93	12,31	1,63	32,99	12,98	0,08
ICl	26,23	27,42	2,32	25,56	10,92	0,09
<b>Average</b>					12,07	0,11

**Table 5**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
LiH	7,36	0,88	1,59	21,48	22,90	0,07
NaH	8,83	0,97	1,89	20,93	21,70	0,02
KH	10,46	0,98	2,24	19,79	20,98	0,02
RbH	11,01	0,99	2,37	19,66	20,70	0,03
CsH	11,55	1,00	2,49	19,39	20,43	0,04
<b>Average</b>					21,34	0,03

**Table 6**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BeH	5,03	0,91	1,34	25,11	19,72	0,05
MgH	6,98	0,97	1,73	23,72	19,95	0,06
CaH	7,94	0,98	2,00	21,4	18,55	0,02
SrH	8,53	0,99	2,15	20,96	18,26	0,03
BaH	8,77	1,00	2,23	20,62	17,86	0,05
<b>Average</b>					18,87	0,04

**Table 7**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BH	4,41	0,92	1,23	25,39	18,84	0,03
AlH	6,16	0,97	1,65	22,63	18,03	0,02
InH	7,02	0,99	1,84	21,85	17,93	0,02
TlH	7,43	1,00	1,87	21,87	18,58	0,01
<b>Average</b>					18,34	0,02

**Table 8**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
CH	3,66	0,93	1,11	28,32	18,19	0,03
SnH	6,33	0,99	1,79	24,13	17,46	0,01
PbH	6,65	1,00	1,84	22,57	17,18	0,02
<b>Average</b>					17,61	0,02

**Table 9**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (A)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
NH	3,03	0,94	1,04	31,92	16,98	0,018
BiH	6,11	1,00	1,81	23,57	16,39	0,018
<i>Average</i>					16,68	0,018

**Table 10**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (A)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
HF	2,53	0,96	0,92	37,41	17,17	0,10
HCl	3,47	0,98	1,27	30,98	15,36	0,01
HBr	3,91	0,99	1,41	29,15	15,05	0,03
HI	4,48	1,00	1,60	27,10	14,58	0,06
<i>Average</i>					15,54	0,05

**Table 11**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (A)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
ZnH	6,6	0,99	1,59	23,83	20,37	0,04
CdH	7,47	0,99	1,76	23,26	20,57	0,05
HgH	8,21	1,00	1,74	13,97	17,63	0,10
<i>Average</i>					19,52	0,07

**Table 12**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
CsF						
CsBr	52,63	49,92	3,14	19,61	10,50	0,16
CsI	71,63	64,94	3,41	17,72	10,98	0,12
NaCl	26,46	13,95	2,51	21,68	13,14	0,05
NaBr	31,98	17,86	2,64	20,80	13,07	0,04
NaI	35,15	19,45	2,90	18,75	11,90	0,05
KF	25,64	12,78	2,55	27,66	14,79	0,18
KCl	35,95	18,59	2,79	21,72	13,93	0,11
KBr	43,55	26,26	2,94	20,11	12,96	0,03
KI	47,48	29,89	3,23	18,12	11,45	0,09
RbCl	39,53	25,07	2,89	21,09	12,55	0,00
<b>Average</b>					12,57	0,08

**Table 13**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BeO	6,83	5,77	1,33	79,26	19,03	0,02
MgO	12,90	9,59	1,75	75,10	20,63	0,10
BaO	15,00	14,33	1,94	68,64	16,92	0,10
SrO	15,50	13,53	1,92	69,95	18,36	0,02
<b>Average</b>					18,73	0,06

**Table 14**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BeF	8,00	6,11	1,36	32,14	13,49	0,02
BeCl	12,00	7,17	1,70	26,58	13,59	0,03
MgF	14,10	10,60	1,75	29,26	13,39	0,02
CaF	17,20	12,88	2,02	26,68	12,25	0,07
<b>Average</b>					13,18	0,04

**Table 15**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BO	5,37	6,52	1,20	91,27	16,74	0,03
AlO	10,37	10,04	1,62	77,28	17,76	0,03
<i>Average</i>					17,25	0,03

**Table 16**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
BF	7,26	6,72	1,26	30,01	12,18	0,07
BCl	12,06	8,38	1,72	25,25	12,17	0,07
BBr	14,77	9,66	1,88	24,20	12,43	0,09
AlCl	20,95	15,24	2,13	22,04	6,44	0,44
AlBr	26,64	20,11	2,29	20,19	11,67	0,02
InCl	31,71	26,82	2,31	23,28	12,79	0,12
InI	56,72	60,32	2,86	18,93	11,11	0,03
TlCl	35,09	29,87	2,55	22,81	12,03	0,05
TlBr	52,27	57,98	2,68	21,10	11,77	0,03
TlI	66,67	78,31	2,87	19,19	11,50	0,01
<i>Average</i>					11,41	0,09

**Table 17**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ◦ (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
CO	4,67	6,86	1,13	94,28	15,32	0,00
CS	7,86	8,73	1,53	77,13	15,27	0,00
SiO	8,13	10,18	1,51	80,63	15,15	0,00
SiS	13,43	14,93	1,93	64,79	14,49	0,05
GeO	10,23	13,15	1,65	79,47	15,24	0,00
SnO	12,27	14,09	1,84	76,30	15,52	0,02
SnS	20,62	25,25	2,06	58,65	15,26	0,00
PbO	14,00	14,85	1,92	75,47	16,44	0,08
PbS	23,49	27,72	2,39	60,82	14,56	0,05
<i>Average</i>					15,25	0,02



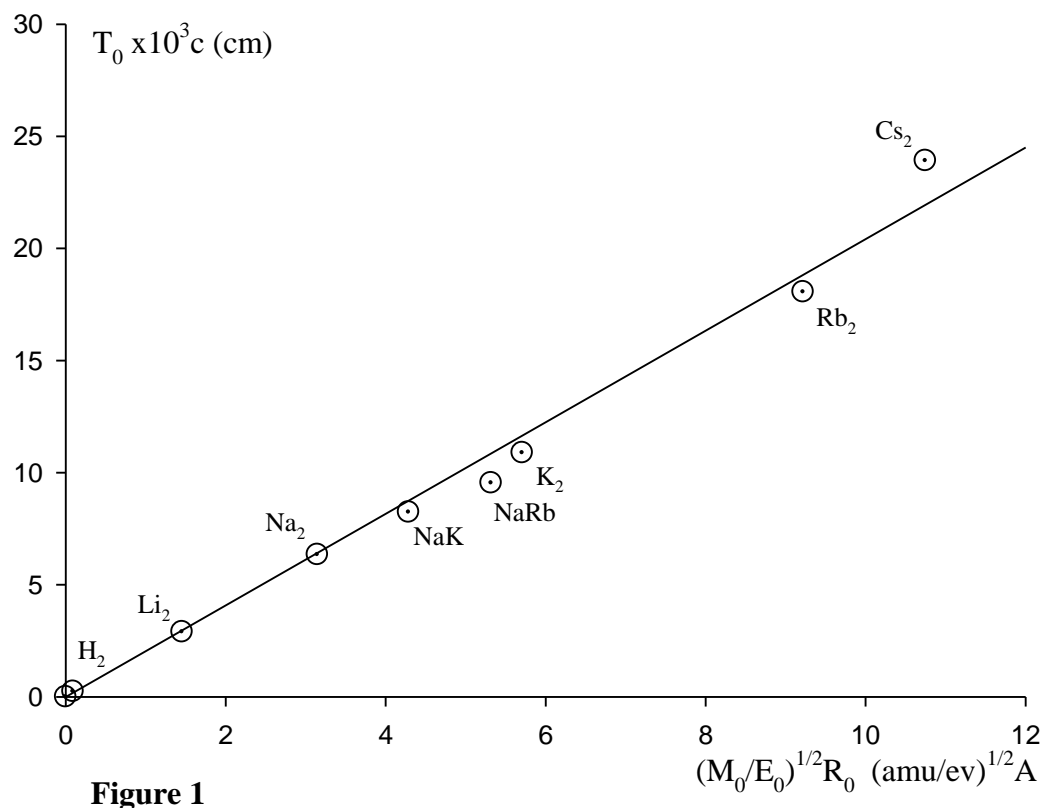
**Table 18**

Molecules	$T_0$ ( $\text{cm}^{-1}$ $\times 10^4 \text{c}$ )	$M_0$ (amu)	$R_0$ ° (Å)	E (ev)	$\frac{T_0}{R_0} \sqrt{\frac{E_0}{M_0}}$	RelativeError  as Referred to the Average
NO	5,33	7,47	1,15	98,21	16,81	0,02
PO	8,21	10,55	1,45	85,15	16,09	0,02
<i>Average</i>					16,45	0,02

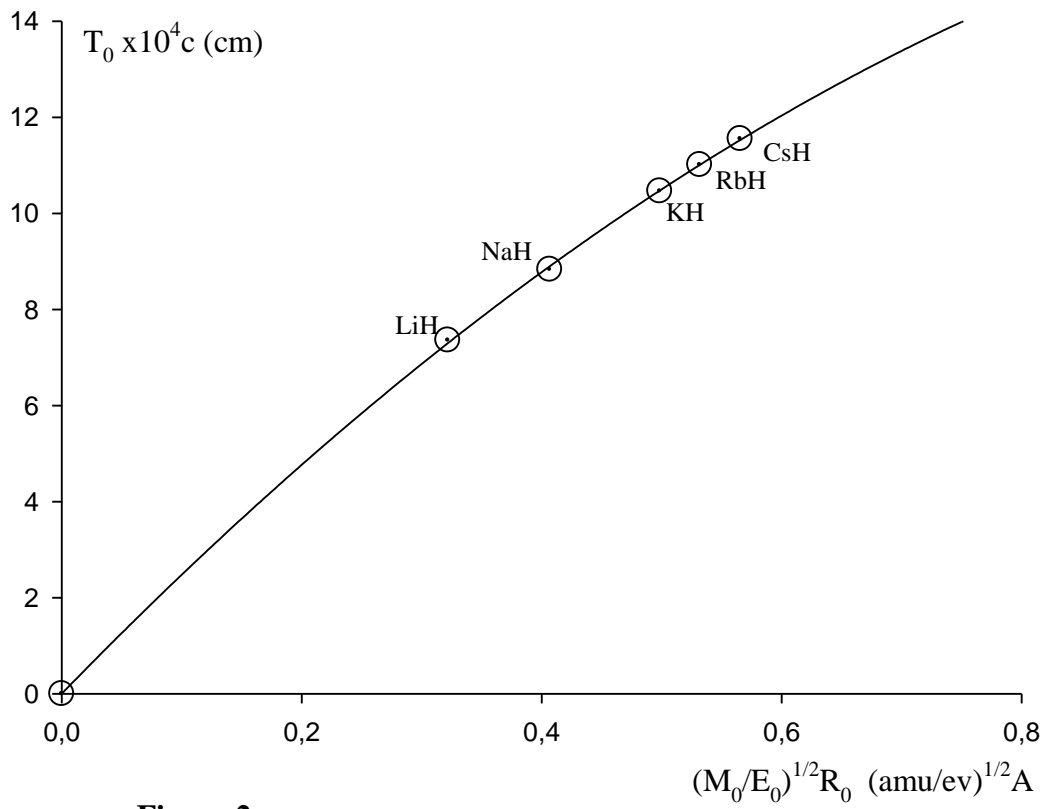
**Table 19**  $g_k$ 's

Family of	<b>H<sub>2</sub></b>	<b>N<sub>2</sub></b>	<b>O<sub>2</sub></b>	<b>F<sub>2</sub></b>	<b>LiH</b>	<b>BeH</b>	<b>BH</b>	<b>CH</b>	<b>NH</b>
$g_k$	1.01	1.06	0.64	0.32	1.10	0.93	0.90	0.82	0.74

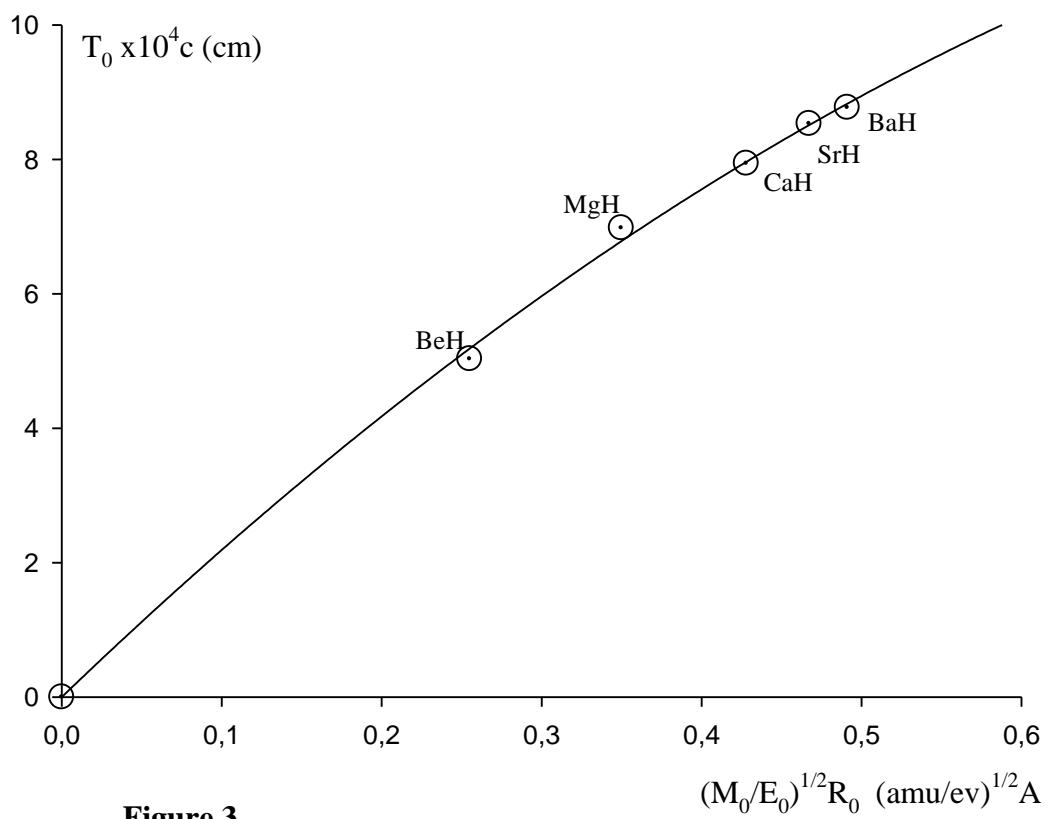
Family of	<b>HF</b>	<b>ZnH</b>	<b>CsF</b>	<b>BeO</b>	<b>BeF</b>	<b>BO</b>	<b>BF</b>	<b>CO</b>	<b>NO</b>
$g_k$	0.62	0.99	0.37	0.91	0.45	0.83	0.36	0.62	0.72



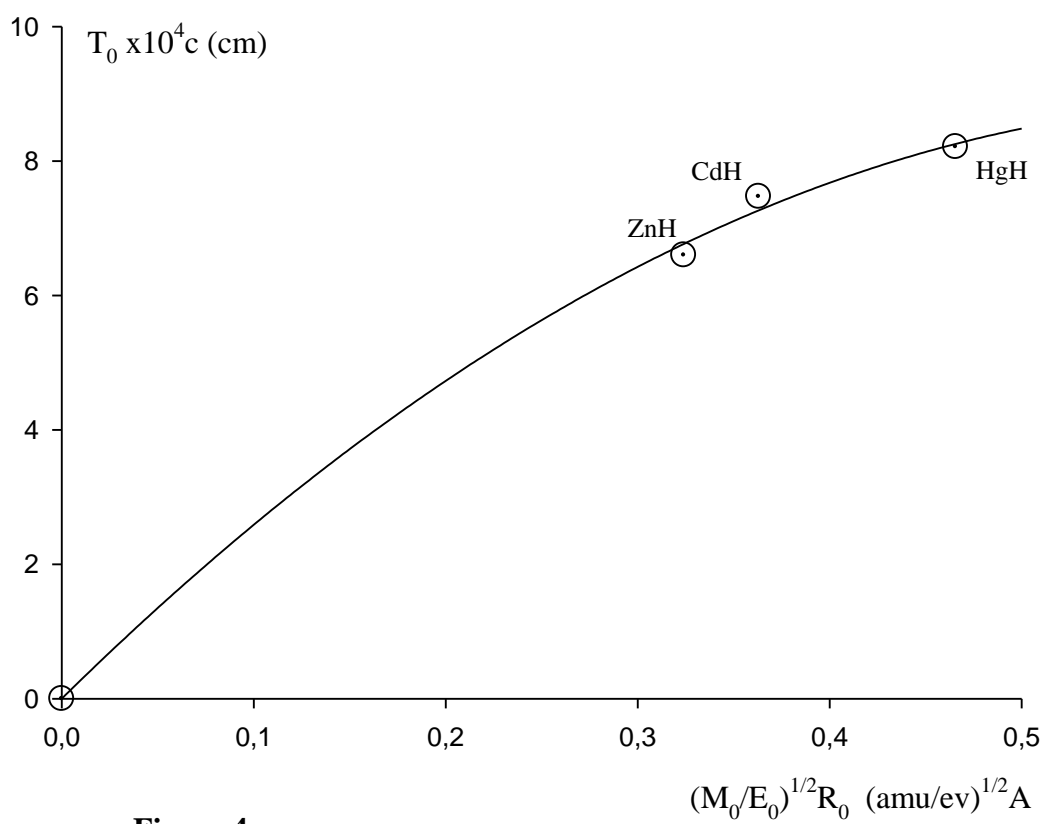
**Figure 1**



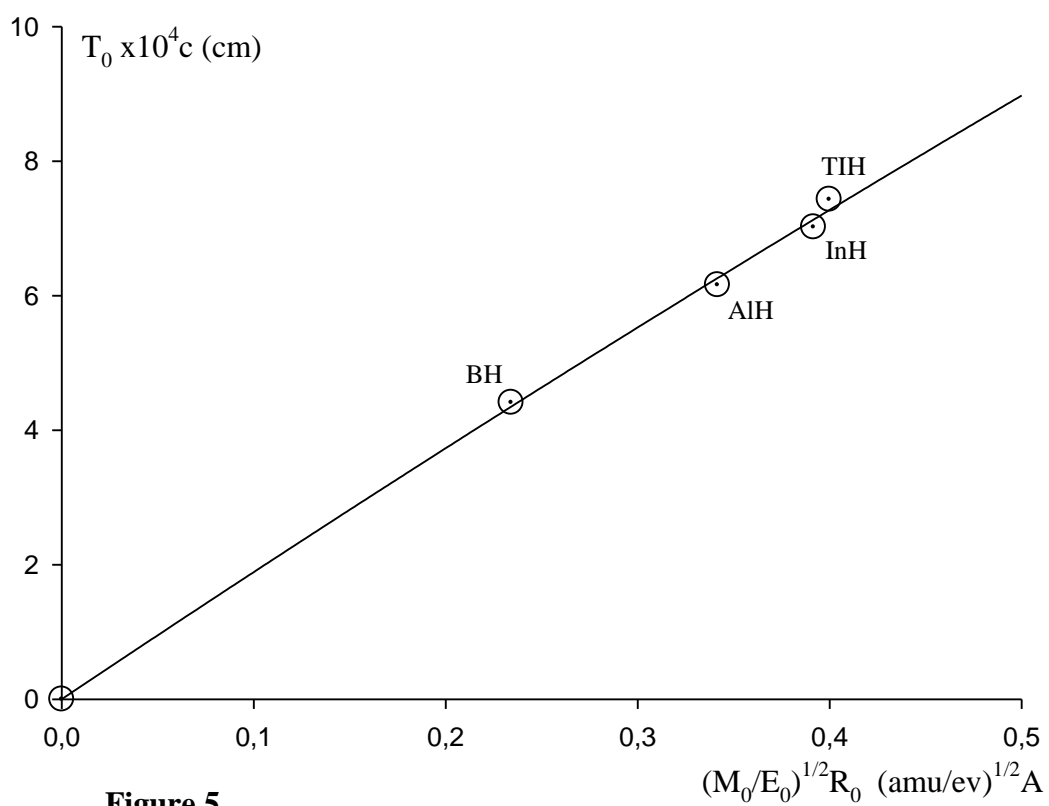
**Figure 2**



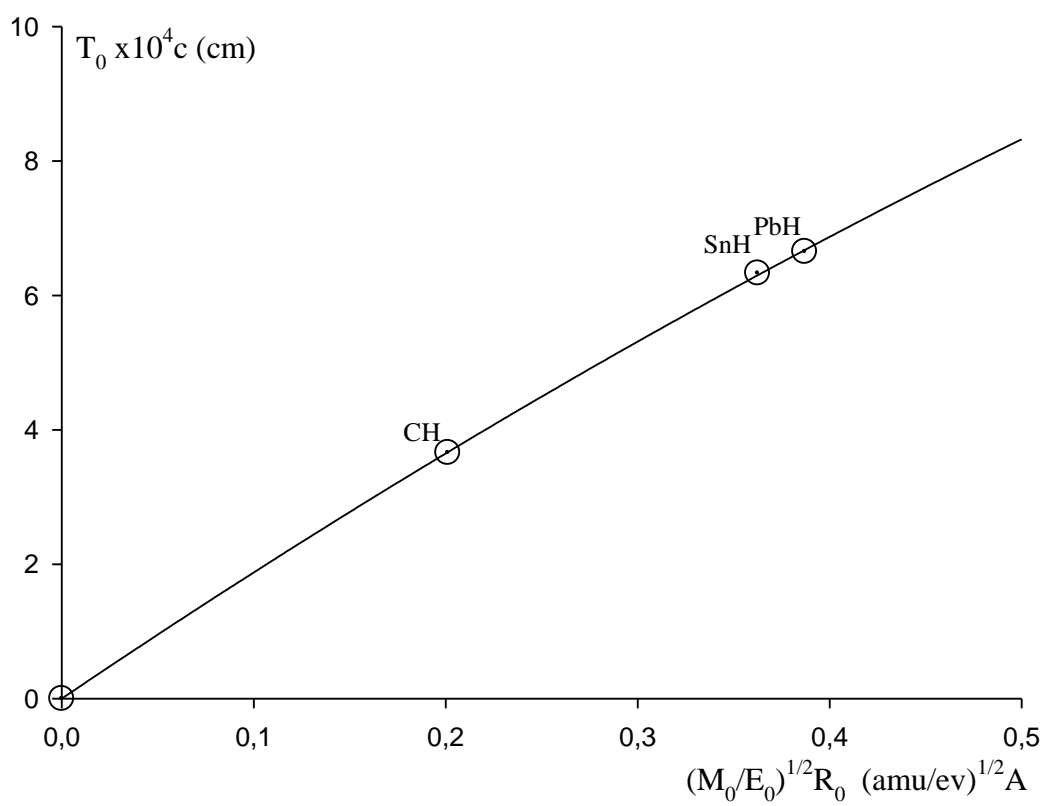
**Figure 3**



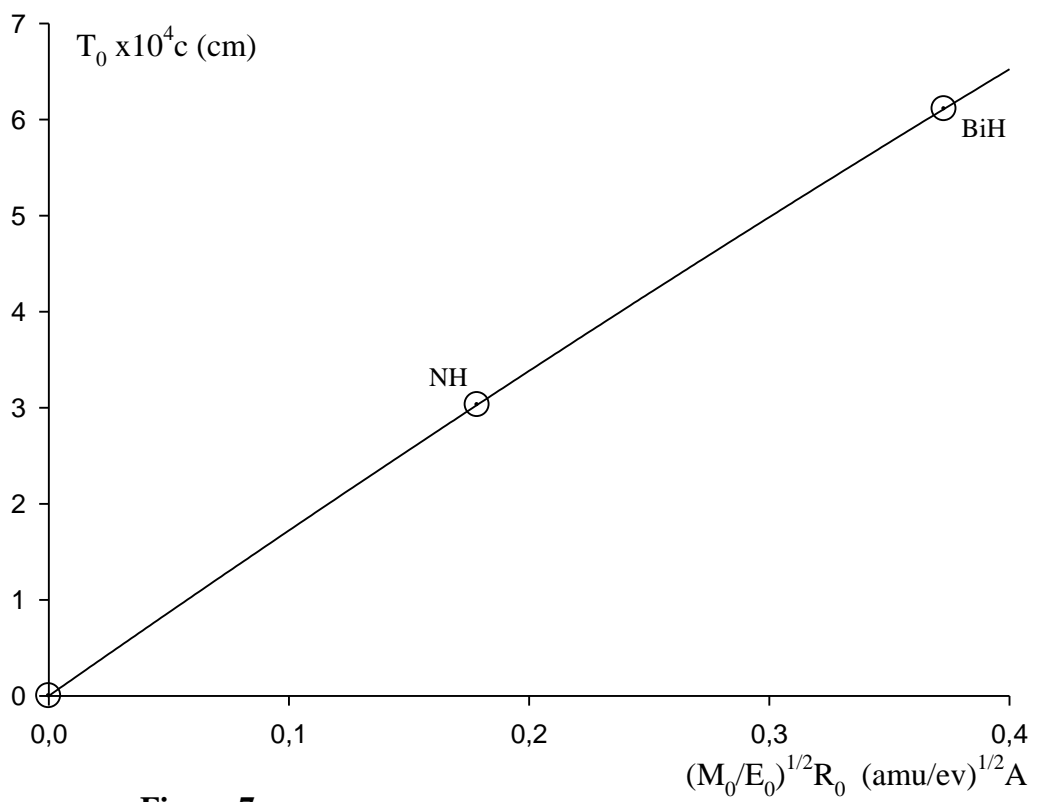
**Figure 4**



**Figure 5**

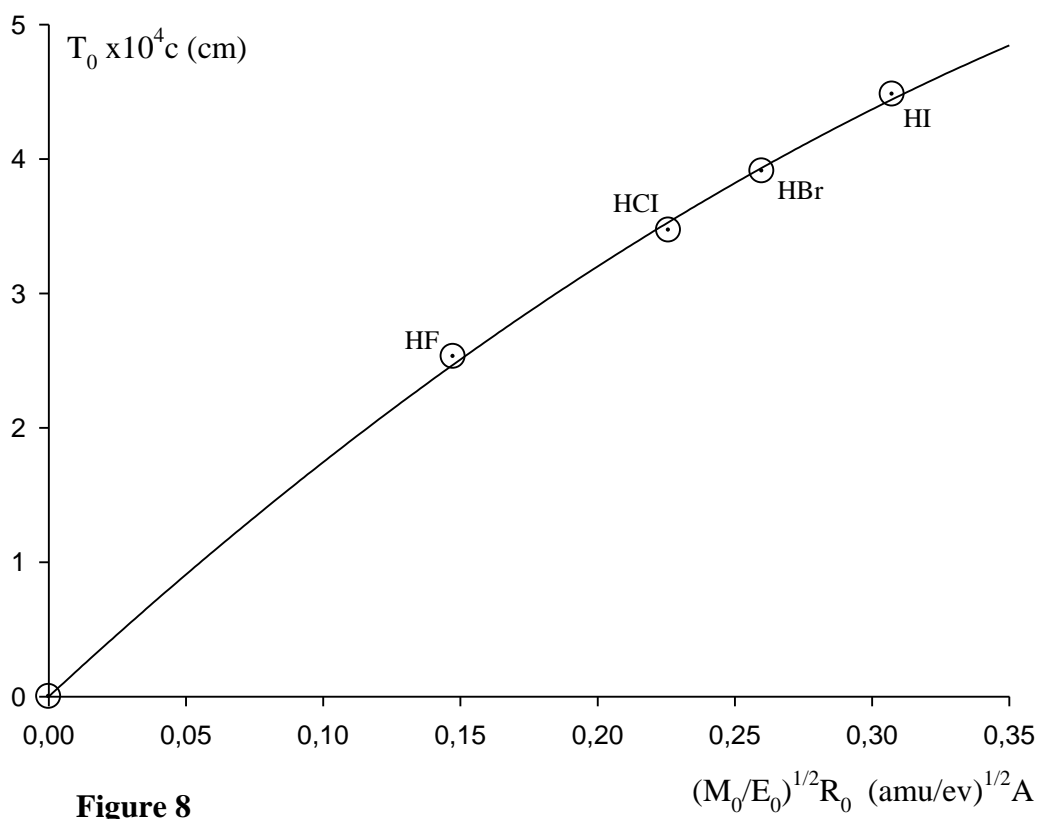


**Figure 6**

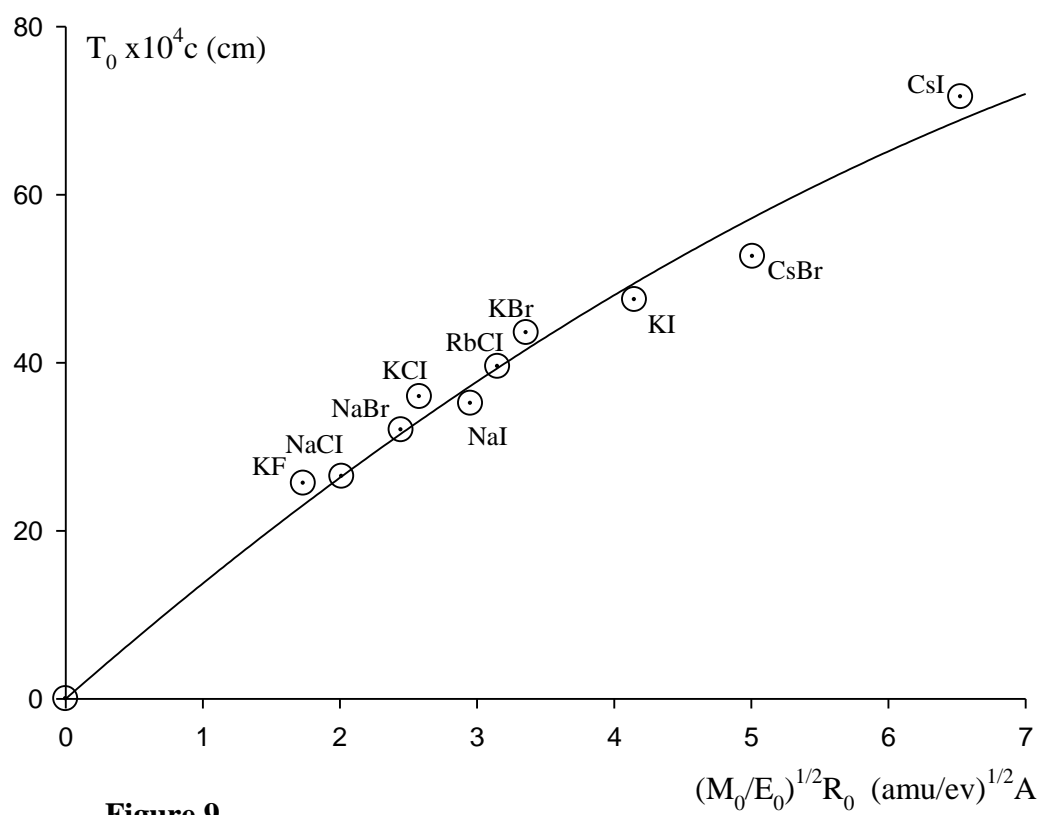


**Figure 7**

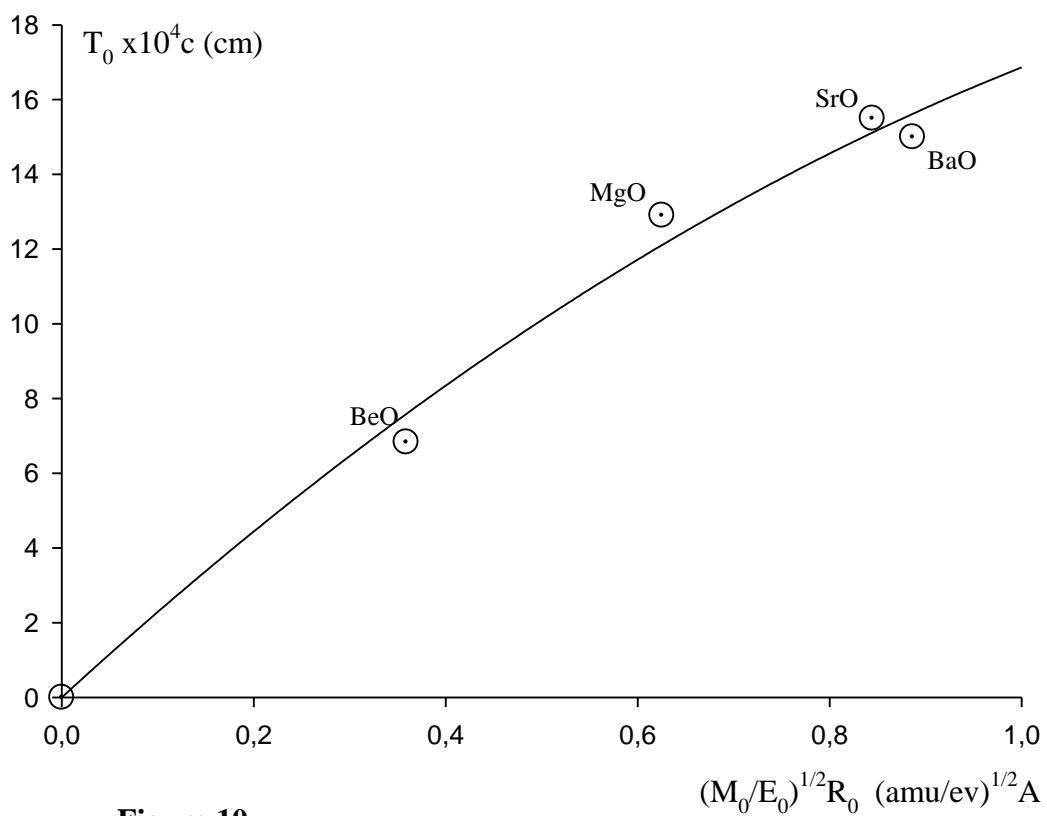




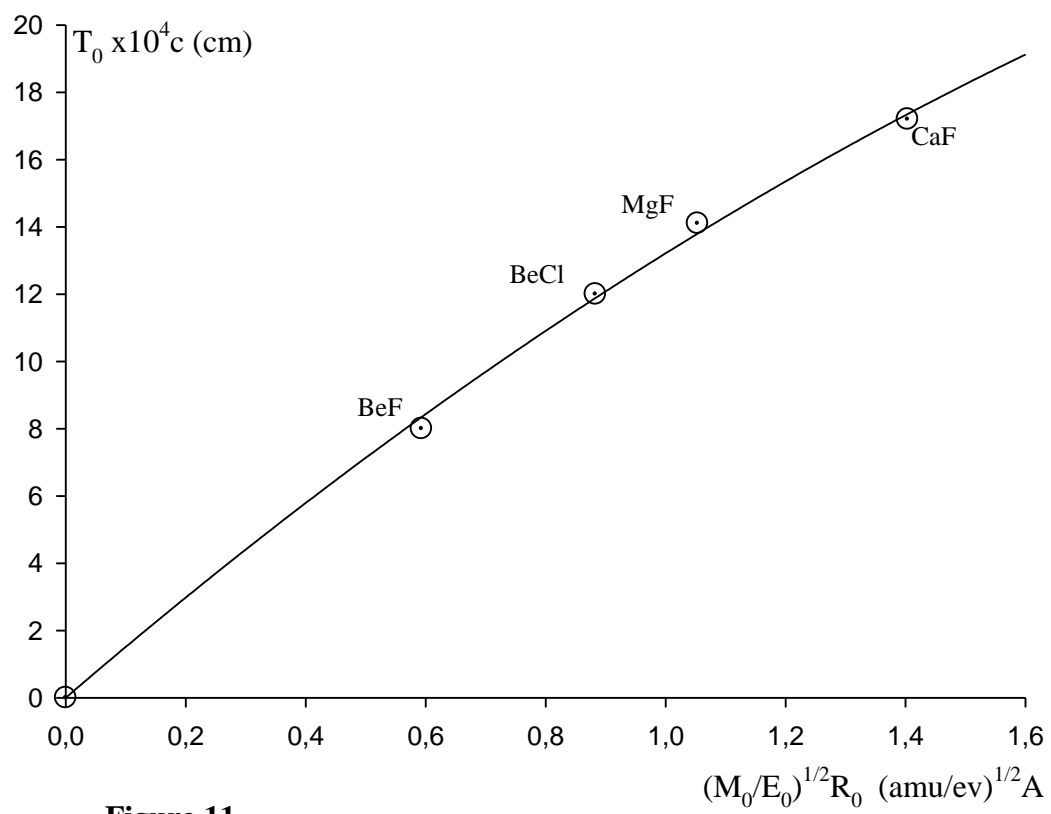
**Figure 8**



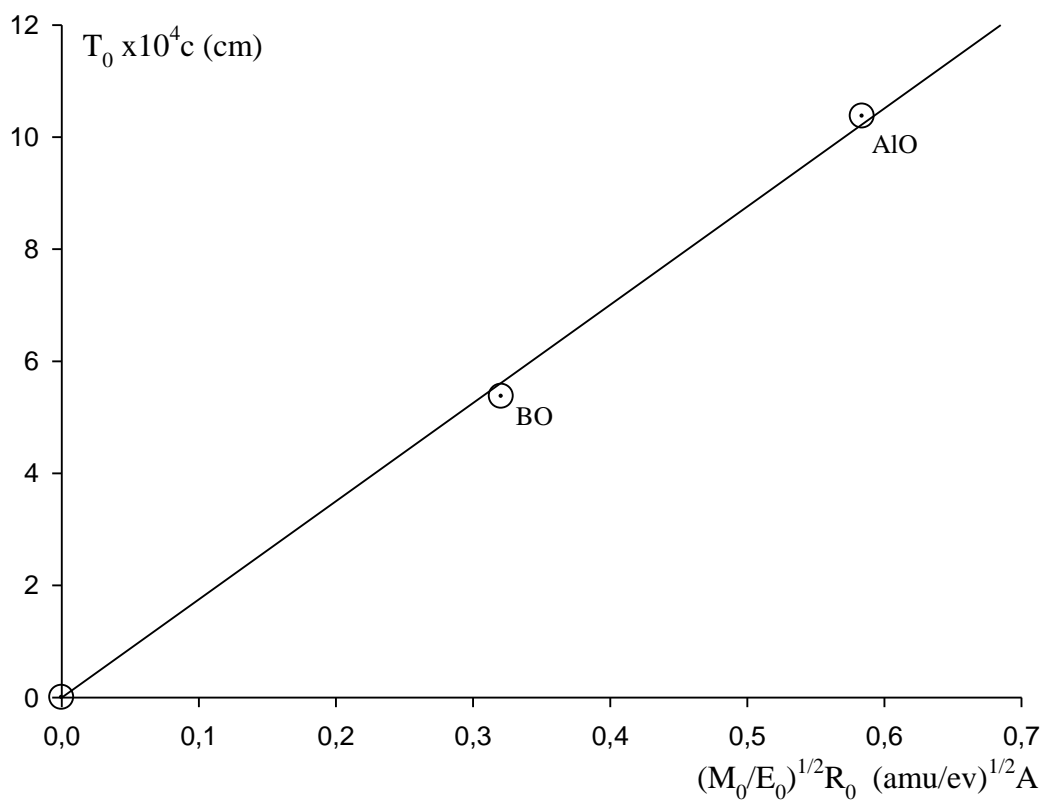
**Figure 9**



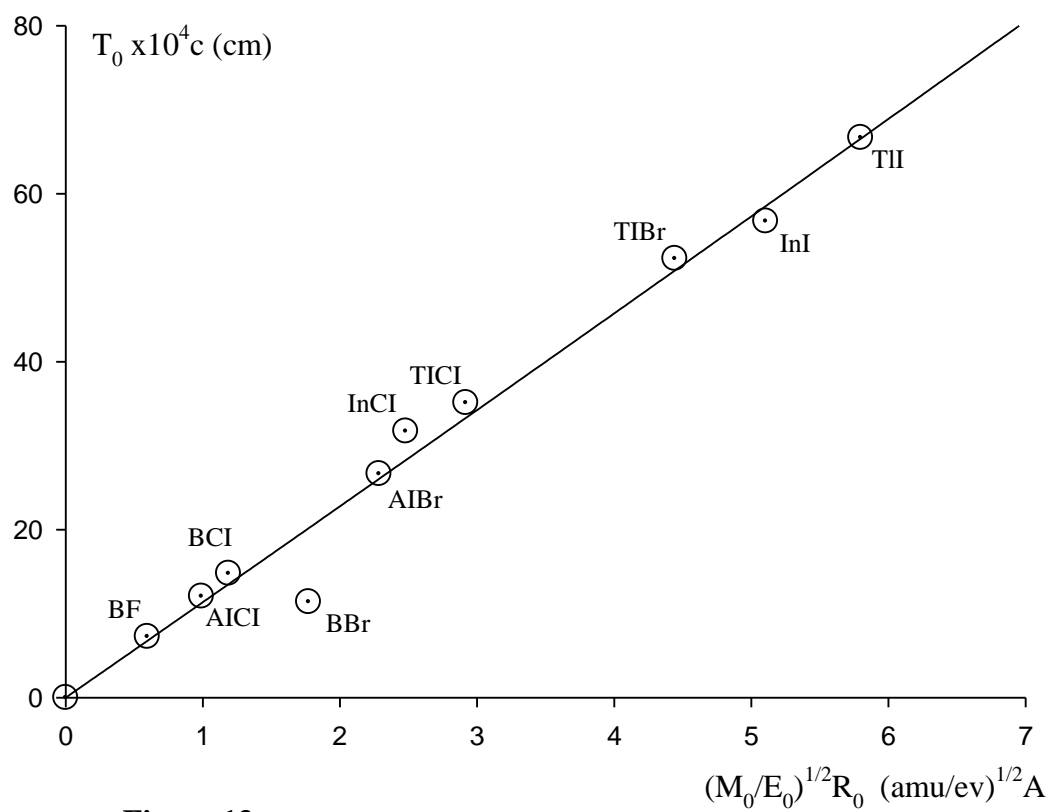
**Figure 10**



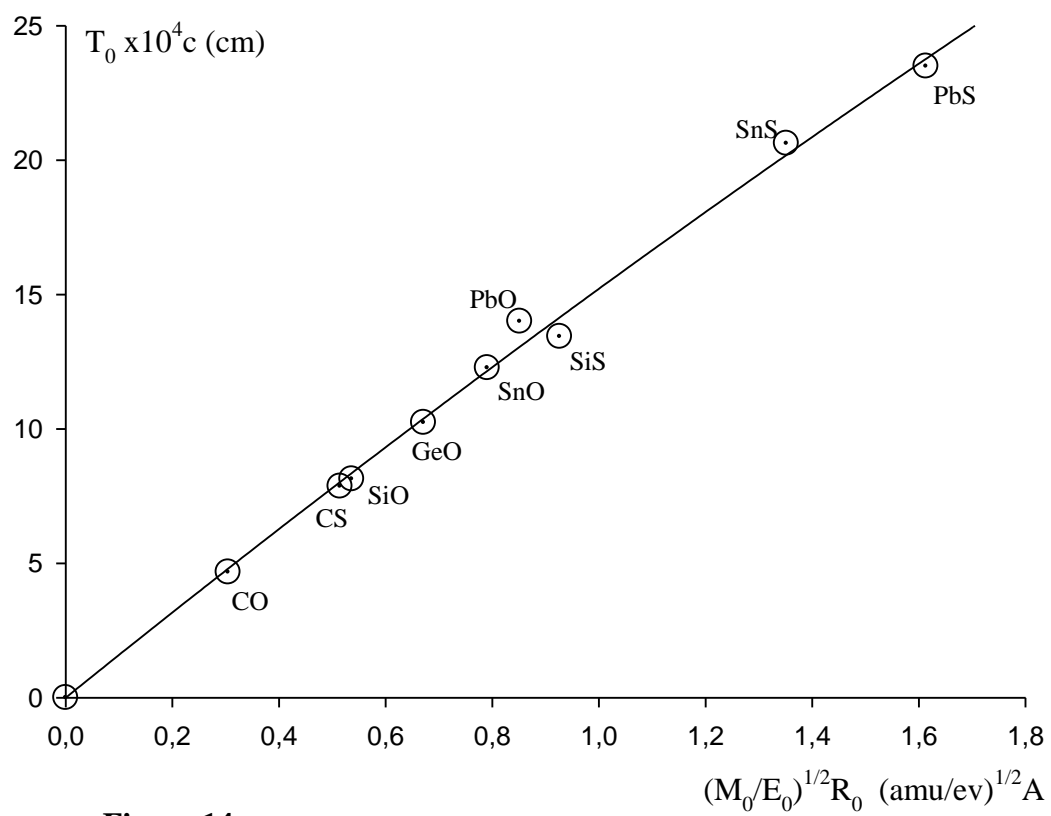
**Figure 11**



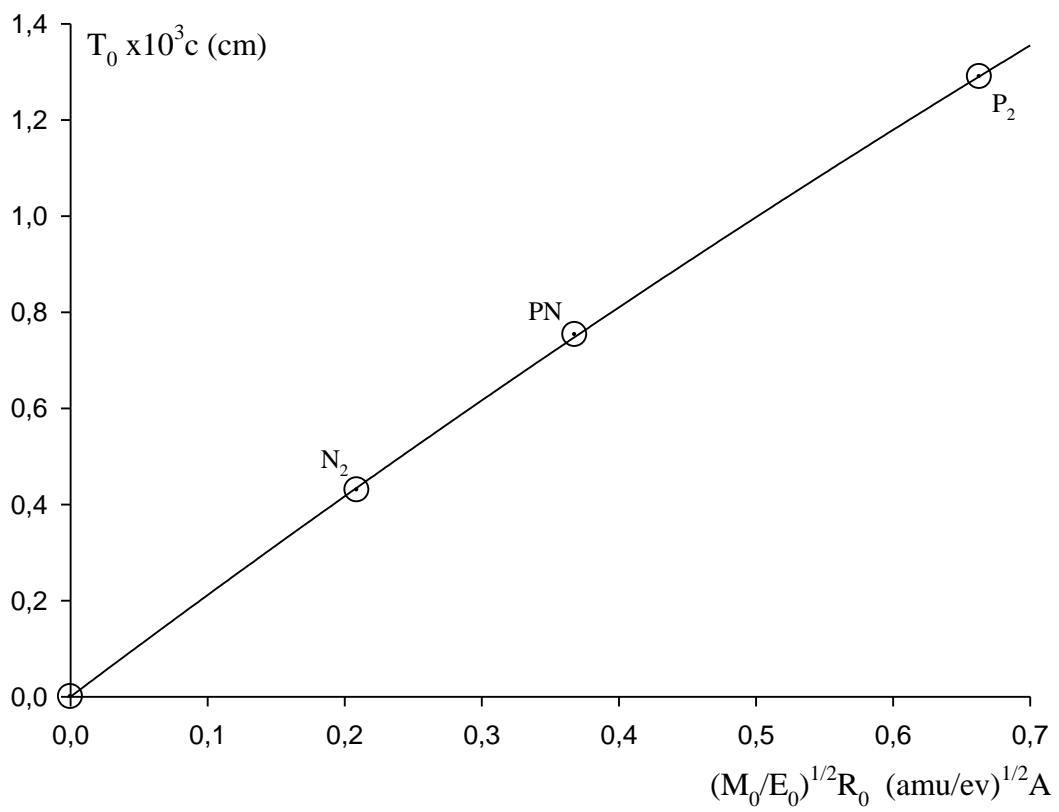
**Figure 12**



**Figure 13**

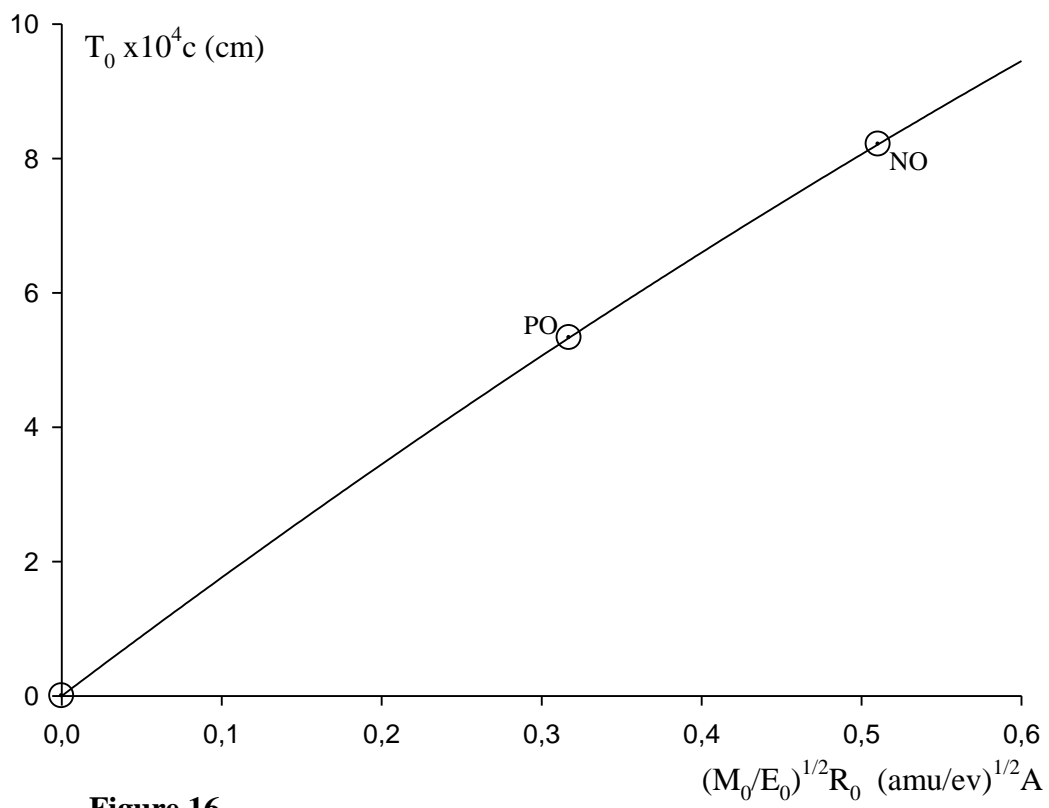


**Figure 14**

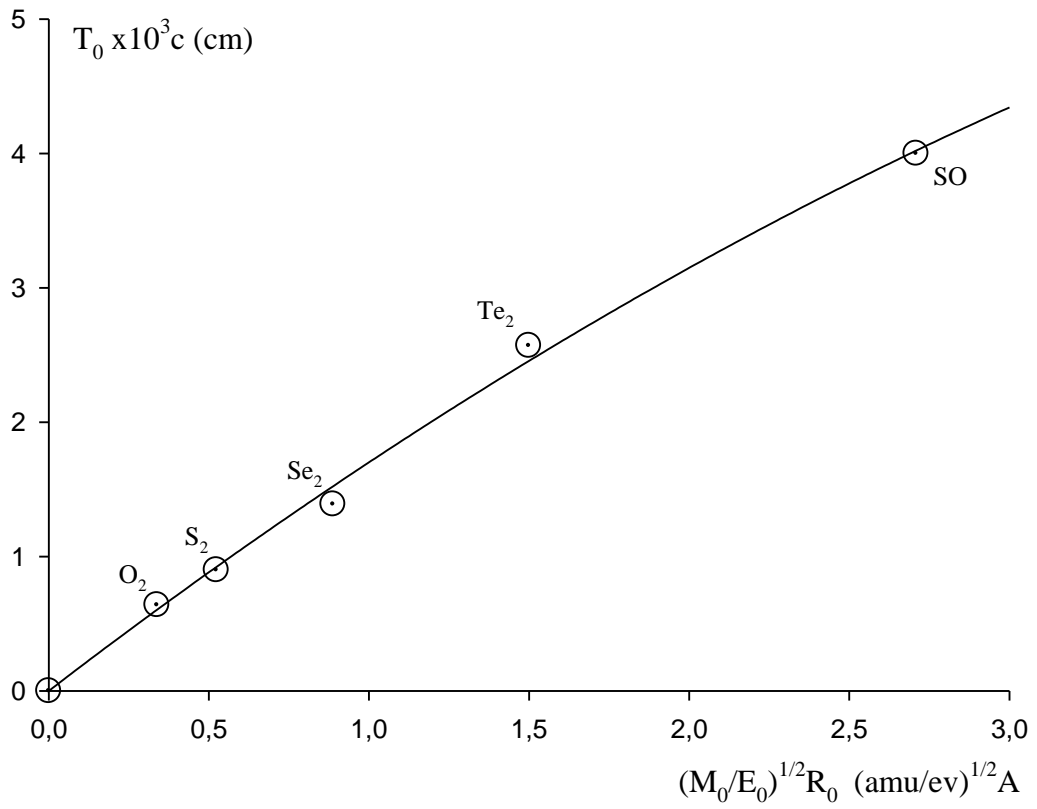


**Figure 15**

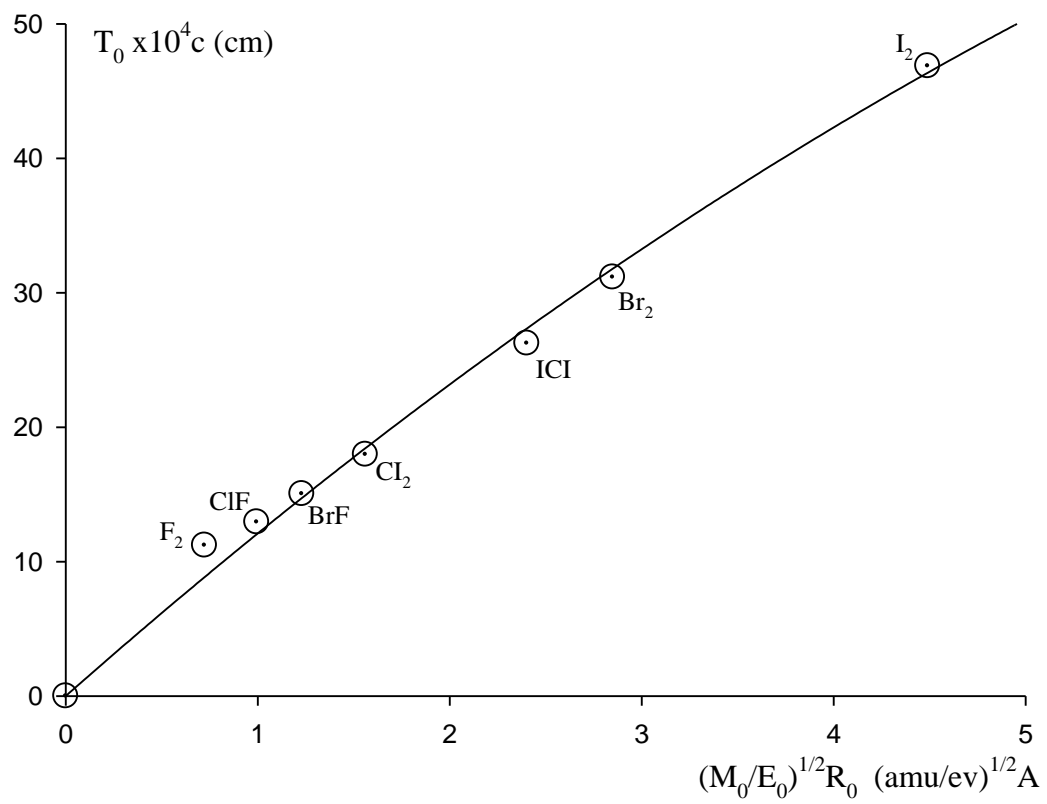




**Figure 16**



**Figure 17**



**Figure 18**

## CONCLUSION

The foregoing results show that our prediction, i.e Eq.(6), together with the *constancy of the coefficient  $g_k$ , for members of a given chemical family*, indeed holds fairly successfully. The constant  $(T_0/R_0)(\sqrt{M_0/E_0})\{(cm^{-1} \times 10^3 c/A)\sqrt{amu/ev}\}$ , i.e.  $\sqrt{g_k}$ , varies between, approximately 1 and 2, throughout different families.

One can show that  $g_k$  happens to be roughly, *inversely proportional to the dissociation energy of the molecule*.<sup>13</sup> As one can observe from Table 19, it indeed decreases as the bond becomes stronger. Thus, the smaller  $g_k$  is, the higher is the number of the covalent bonds, making the overall bond of the diatomic molecule, or the higher is the number of free electrons an atom possesses, the looser will be the bond it will make with, say, an halogen, thus the higher will  $g_k$  be, etc.

It is easy to check that, Eq.(6) amazingly holds, even for the Bohr hydrogen atom, for which however,  $g_k$  becomes unity.

Note that we have found nothing similar to the line we pursued herein.

## ACKNOWLEDGEMENT

The author would like to extend his special gratitude to Professor V. Rozanov. He would like to further thank to Drs. N. Veziroğlu, O. Sinanoğlu, E. Hasanov, C. Marchal, Ş. Koçak, for very many hours of discussions, which helped a lot to improve the work presented herein.

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